

Knuth-Morris-Pratt (KMP) Algorithm

Concepts

String: ABCDE

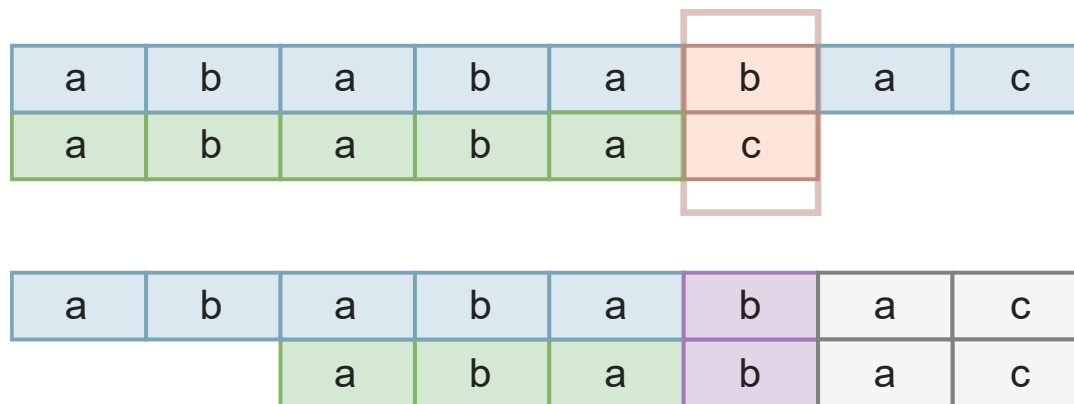
Proper prefixes: <NULL>, A, AB, ABC, ABCD

Proper suffixes: <NULL>, E, DE, CDE, BCDE

Substring of interest: Largest common substring that is both prefix & suffix

Failure function: The length of the longest prefix of **P** that is a suffix of $P[1..j]$ and $f(0) = 0$

Intent: Upon mismatch, shift the string so that prefix replaces suffix



Working example of KMP search using failure function

a b a c a a b a c c a b a c a b a a b b

1 2 3 4 5 6
a b a c a b

7
a b a c a b

8 9 10 11 12
a b a c a b

13
a b a c a b

14 15 16 17 18 19
a b a c a b

no comparison
needed here

j	0	1	2	3	4	5
$pat[j]$	a	b	a	c	a	b
$f(j)$	0	0	1	0	1	2

Another example of KMP search

Step 1	A	B	C	A	B	C	D	A	B	A	B	C	D	A	B	C	D	A	B	D	E
	A	B	C	D	A	B	D														
Step 2	A	B	C	A	B	C	D	A	B	A	B	C	D	A	B	C	D	A	B	D	E
				A	B	C	D	A	B	D											
Step 3	A	B	C	A	B	C	D	A	B	A	B	C	D	A	B	C	D	A	B	D	E
								A	B	C	D	A	B	D							
Step 4	A	B	C	A	B	C	D	A	B	A	B	C	D	A	B	C	D	A	B	D	E
										A	B	C	D	A	B	D					
Step 5	A	B	C	A	B	C	D	A	B	A	B	C	D	A	B	C	D	A	B	D	E
														A	B	C	D	A	B	D	

<i>j</i>	0	1	2	3	4	5	6
<i>pat</i> [<i>j</i>]	A	B	C	D	A	B	D
<i>f</i> (<i>j</i>)	0	0	0	0	1	2	0

Reference: <https://blog.devgenius.io/string-matching-kmp-ccad1ffbeb11>

Complexities?